

		Addition	
	Concrete	Pictorial	Abstract
Combinin	Use part part-whole model.	Use pictures to add two numbers together as a	Use the part part-whole diagram.
g two	Use cubes to add two numbers together as a	group or in a bar.	
parts to make whole: part- whole model	group.	Use pictures to add two numbers together as a group or in a bar.	5
Starting	Start with the larger number on the bead string and	Start at the larger number on the number line	Place the larger number in your head
at the	then count on to the smaller number.	and count on in ones or in one jump to find the	and count on the small number to find
bigger		answer.	your answer.
number			
and		6+3=9 < 	
counting		0 1 2 3 4 5 6 7 8 9 10	
on,			
including			
adding a			
2-digit			





number			
and ones	Counting on using number lines by using cubes		
Represen	Some children may need to initially use real objects		Part-whole model to be used
t and use	before moving onto the representations		alongside abstract.
number		6+4=10	
bonds	6+4=10	(10) 4 + 6 = 10	
and us	4+6=10 10-4=6	10-4=6	
related		<u> </u>	
subtractio	Tens Frame		
n facts			
within 20		Part Whole Model	
Regroupi	Start with the bigger number and use the smaller	Use pictures or a number line. Regroup or	Part-whole model to be used
ng to	number to make 10. Use ten frames.	partition the smaller number using the part	alongside abstract.
make 10	6 + 5 =	part-whole model to make 10.	
This is an			
essential		9 + 5 - 14	
skill for			
column			
addition		0 1 2 3 4 5 6 7 6 9 10 11 12 13 14 15 16 17 16 18	
later on			
Add a 2	Explore that the ones digit does not change.	Dienes may be used, as well as a number line.	Focusing on the place value column,
digit			children add that amount of tens.







number and tens	25 + 1 0 = 35	27 + 30 +10 +10 +10 27 37 47 57	Children should be able to mentally add a ten to a number.
Add two 2 digit numbers	Model using dienes and place value counters. Image: Counter state of the state of t	Use a number line and bridge ten using part- whole if necessary. $\begin{array}{r} +20 & +5 \\ \hline 47 & 67 & 72 \end{array} \xrightarrow{Or} +20 & +3 & +2 \\ \hline 47 & 67 & 70 & 72 \end{array}$	Partition the number into columns to support the place value in preparation for formal written methods. Children should be able to mentally add each part in their head. 47 + 35 40 + 7 30 + 5 70 + 12
Add three 1 digit	Combine to make 10 first if possible, or if possible then add third digit.	Regroup and draw representations.	Combine the two numbers that make/ bridge ten, then add on the third.
numbers		इ. इ. इ. इ. इ. इ. इ. इ. इ. इ. इ. इ. इ. इ. इ. इ. इ	4 + 7 + 6 = 10 + 7 = 17



Column	Model using dienes or place value counters.	Children move onto drawing the counters.	Calculations
addition, formal method – no exchangi ng	24 + 15= Add together the ones first then add the tens. Use the Base 10 blocks first before moving onto place value counters.	$ \begin{array}{c} 1 & 2 & 6 & 1 & 1 & 2 & 2 \\ & (2)$	21 + 42 = 21 + <u>42</u>
Column	Make both numbers on a place value grid.	Children can draw a pictorial representations	223
formal		further support their loorning and	
ronnai			+ 1 1 4
		understanding.	
exchangi		• • • • • •	
ng		• •	
			337
	Add up the units and exchange 10 ones for one 10.		
	Add up (a) Add up the rest of the the	7 1 5 1	
		• •	
		·	

























number			Children should be able to mentally
and tens			subtract a ten from a two-digit number.
Subtract	Model using dienes and place value counters.	Use a number line and bridge ten using part-	Partition the number into columns to
two 2		whole if necessary.	support the place value in preparation
digit			for formal written methods. Children
numbers,			should be able to subtract 2 two-digit
no			numbers mentally.
exchange			
Column	Use dienes to make the bigger number and then	Draw the dienes or place value counters	
subtractio	take the smaller number away. Show how you	alongside the written calculation to help to	[▶] H T O
n, formal	partition numbers to subtract.	show working.	er F
method –	Tera Onas	Calculations	
no	///	54	
exchangi		$-2^{\prime}2$	
ng		32	
			act
			eds























Counting	Count the groups as children are skip counting,	Children make representations to show	Count in multiples of a number aloud.
in	children may use their fingers as they are skip	counting in multiples.	
multiples	counting.	my and my and and and	2, 4, 6, 8, 10
		Use a number line or pictures to continue support in counting in multiples.	5, 10, 15, 20, 25
Repeated	Use difference objects to add equal groups.	Use pictorial representations, including a	Write addition sentences to describe
addition		number line.	objects and pictures.
		3+3+3+3+3 = 15	2+2+2+2=10





Arrays –	Create arrays using counters, cubes and numicon.	Use representations of arrays to show different	Use an array to write multiplication
showing	Pupils should understand that an array can	calculations and explore commutativity.	sentences and reinforce repeated
multiplicat	represent different equations and that, as		addition.
ion is	multiplication is commutative, the order of the	~ ~ ~ ~	00000
commutat	multiplication does not affect the answer.		00000
ive			00000
			5 + 5 + 5 = 15
			5+5+5=15
			3 + 3 + 3 + 3 + 3 = 15
		$\bigcirc \bigcirc \bigcirc \bigcirc \bigcirc \bigcirc$	5 x 3 = 15
			3 x 5 = 15
Using	5=1×5 • • • • •		
known			
facts for	50 = 10 × 5		
multiplyin	500 = 100 × 5		
g	5000 = 1000 × 5 🚺 🚺 🚺 🚺		
multiples	3 × 2 = 6 30 × 2 = 60 300 × 2 = 600 3000 × 2 = 6000		
of 10, 100			
and 1000.	: = 2 1		
	: = =		





















23 2 With th x 23 = 1 Why is 0	23 23 23 23 23 23 ? ne counters, prove that 6 38 6 x 23 = 32 x 6?	Mai had to swim 23 times a week. How r did she swim in one Tom saved 23p thre week. How much did weeks?	lengths, 6 many lengths week? e days a d he save in 2	Find the product of 6 and 23 $6 \times 23 =$ $= 6 \times 23$ $= 6 \times 23$ $\times 23 =$ $\times 23 \times 6$ = -	What's the calculation? What's the answer?
			Divisio	n	
	Concre	te		Pictorial	Abstract
Division as sharing (sharing objects into group	10 10 10 10 10 10 10 10 10 10	10 , can you them y in 2 s?	80 This can also have a similar	be done in a bar so all 4 operations structure:	6 ÷ 2 = 3 What's the calculation?
Division as grouping and repeated	Divide quantities into equal g	roups.		3 4 5 6 7 8 9 10 11 12 3 3 3 3 3	28 + 7 = 4 Divide 28 into 7 groups. How many are in each group?





subtractio	10	
n		
	0 5 10 15 20 25 30 35	
	96 + 3 = 32	
	Ö • ö • ö •	
Division	Link division	
with		
arrays	multiplication	
including	an array and	
fact	thinking	
families	about the	
and	number sentences that can be created.	
inverse	Eq 15 + 3 = 5 5 x 3 = 15	Draw an array and use lines to split the array into group to make multiplication and division sentences.
	15 + 5 = 3 3 x 5 = 15	





Division	Use of lollipop sticks to form wholes		
with a			
remainde			
r			
		-1 - 4 - 4	
		660000000000000000000000000000000000000	
Using			
known			
facts for			
dividing			
multiples			
of 10, 100			
and 1000			











tototo $2)58$ $2)58$ $2\frac{1}{58}$ $2)58$ $2\frac{1}{58}$ $\frac{4}{18}$ Two goes into 5 two times, or 5 tens + 2 = 2 whole tens but there is a remainder!To find it, multiply $2 \times 2 = 4$, write that 4 under the five, and subtract to find the remainder of 1 ten.Next, drop down the 8 of the ones next to the leftover 1 ten. You combine the remainder ten with 8 ones, and get 18.1. Divide.2. Multiply & subtract.3. Drop down the next digit. $1. Divide.$ $2. Multiply & subtract.$ $3. Drop down the next digit.1. Divide.2. Multiply & subtract.3. Drop down the next digit.1. Divide.2. Multiply 9 \times 2 = 18, write that 18under the 18, and subtract.1. Divide.Divide 2 into 18. Place 9 into thequotient.Multiply 9 \times 2 = 18, write that 18under the 18, and subtract.The division is over since there areno more digits in the dividend. Thequotient is 29$	1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
Two goes into 5 two times, or 5 tens $* 2 = 2$ whole tens but there is a remainder!To find it, multiply $2 \times 2 = 4$, write that 4 under the five, and subtract to find the remainder of 1 ten.Next, drop down the 8 of the ones next to the leftover 1 ten. You combine the remainder ten with 8 ones, and get 18.1. Divide.2. Multiply & subtract.3. Drop down the next digit.1. Divide.2. Multiply & subtract.3. Drop down the next digit.1. Divide.2. Multiply & subtract.3. Drop down the next digit.1. Divide.2. Multiply $9 \times 2 = 18$, write that 18 under the 18, and subtract.The division is over since there are no more digits in the dividend. The quotient is 29	t o 2 2) <u>5</u> 8	2 2) <u>5</u> 8 -4 1	2 9 2) 5 8 <u>- 4 </u> 1 8
1. Divide.2. Multiply & subtract.3. Drop down the next digit. $2\frac{9}{29}$ $2\frac{9}{29}$ $2\frac{9}{29}$ $2\frac{9}{29}$ $2\frac{1}{58}$ $2\frac{9}{58}$ $2\frac{9}{58}$ $2\frac{9}{58}$ $-\frac{4}{18}$ $-\frac{4}{18}$ $-\frac{18}{0}$ 0 Divide 2 into 18. Place 9 into the quotient.Multiply $9 \times 2 = 18$, write that 18 under the 18, and subtract.The division is over since there are no more digits in the dividend. The quotient is 29	Two goes into 5 two times, or 5 tens + 2 = 2 whole tens but there is a remainder!	To find it, multiply $2 \times 2 = 4$, write that 4 under the five, and subtract to find the remainder of 1 ten.	Next, drop down the 8 of the ones next to the leftover 1 ten. You combine the remainder ten with 8 ones, and get 18.
$\frac{1}{2} \frac{9}{2} \frac{9}{58} = \frac{4}{18}$ Divide 2 into 18. Place 9 into the quotient. $\frac{1}{2} \frac{9}{2} \frac{9}{58} = \frac{29}{258} = \frac{29}{258}$	1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
quotion to zo.	2 9 2) 5 8 -4 1 8 Divide 2 into 18. Place 9 into the quotient.	$\begin{array}{r} t & o \\ 2 & 9 \\ 2 & \overline{) 58} \\ -4 \\ 18 \\ -18 \\ 0 \\ \end{array}$ Multiply 9 × 2 = 18, write that 18 under the 18, and subtract.	$\begin{array}{r} t & o \\ \hline 2 & 9 \\ 2 & 5 & 8 \\ \hline -4 \\ \hline 1 & 8 \\ - & 1 & 8 \\ \hline 0 \end{array}$ The division is over since there are no more digits in the dividend. The quotient is 29.
Fluency variation, different ways to ask children to solve 615 ÷	F	luency variation, different ways	to ask children to solve 615 ÷ 5









